

# Resilience Assessment of Hyperconnected Parcel Logistic Networks Under Worst-Case Disruptions

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Joint work with

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Georgia Tech College of Engineering

**H. Milton Stewart School of  
Industrial and Systems Engineering**



**Physical  
Internet  
Center**


# Problem Motivation

- Parcel delivery industry is one of the **fastest growing industries** in the world.
  - Last year, 87 billion parcels were shipped and delivered.
  - Parcel volume is expected to reach 200 billion in next 5 years.


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- Requires intricate planning
  - Network Design
- Moreover, logistics networks designed with only efficiency considerations
  - Not ideal as disruptions occur

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MALAYSIA

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  - Power outages
  - Pandemics

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- Disruptions lead to:
  - Excess pressure on functional resources
  - Late parcel deliveries
  - Increased costs

WATERLOO REGION

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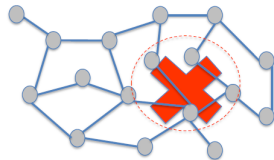
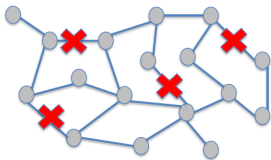
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- **Simulation Models:** Simulation of disruptive events in which the network components fail
  - Random or localized failures
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- **Analytical models:** Estimate the vulnerability of the network through its structural properties
  - Centrality measures
  - Path lengths, edge-disjoint paths

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- Need to also develop a tool to assess resilience of the **large-scale** networks under such **worst-case disruptive events**
    - Intelligent fictitious adversary (Game-theory based)

# Resilient Assessment of Parcel delivery Networks

- **Aim:** To devise a tool that assess the resilience of large-scale logistics networks under worst-case disruptions
  - Through operational costs faced by networks

# Resilient Assessment of Parcel delivery Networks

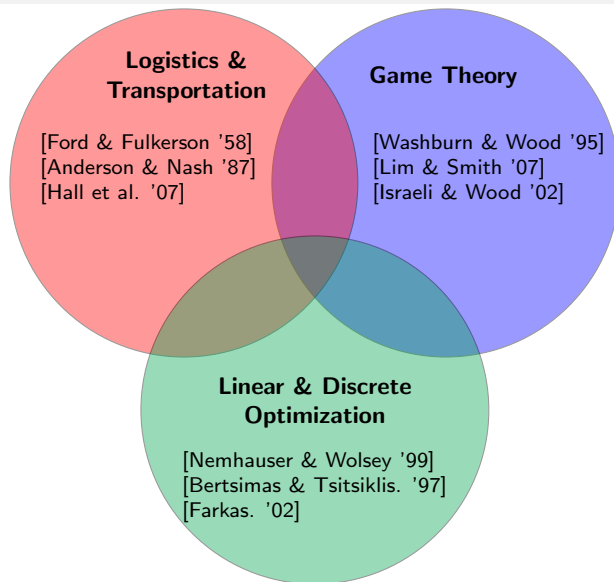
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- We study a **two-person Stackelberg game**:
  - Network components are disrupted to cause most harm (fictitious adversary)
  - Best response to minimize the effects of disruptions (logistics company)
- **Contributions:**
  - Bi-level mixed integer linear program (Network Interdiction Problem)
  - Exact solution technique to assess the resilience
  - Resilience analysis of networks

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- **Agenda:**

To leverage tools from optimization, network science, and game theory to assess the resilience of logistics networks under worst-case disruptions.

# Related Work



- **Goal:**

- ① **Leader:** Interdict edges to maximize the commodity delivery costs between all OD pairs
- ② **Follower:** Minimize the commodity delivery costs after edge-interdiction



# Problem Setting

- **Given:**

- Directed Graph  $\mathcal{G} = (\mathcal{H} \cup \mathcal{S} \cup \mathcal{T}, \mathcal{A})$

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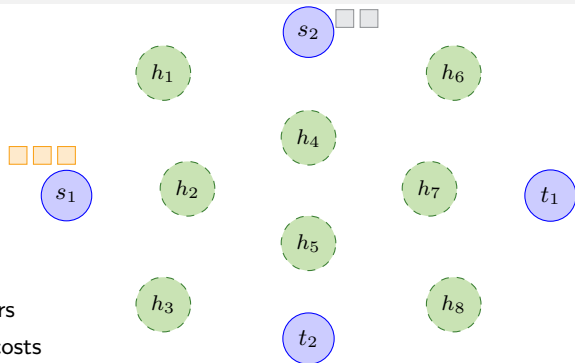
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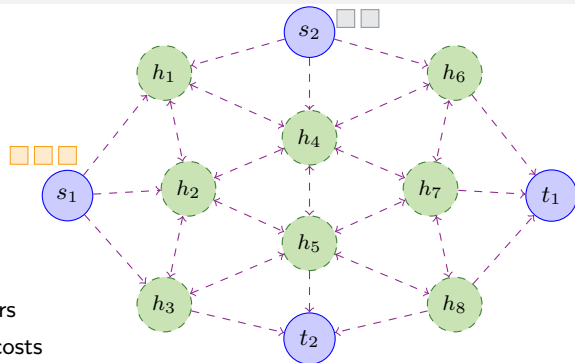
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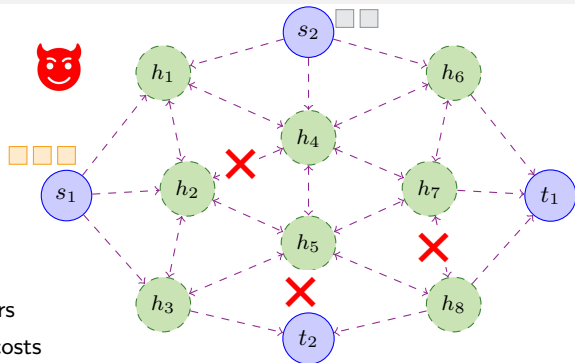
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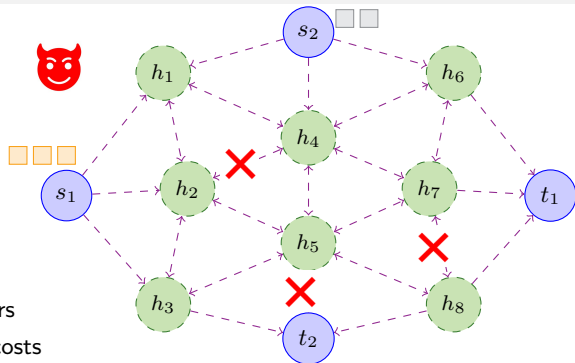
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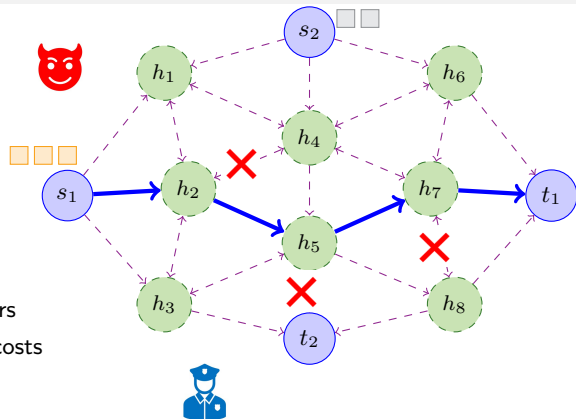
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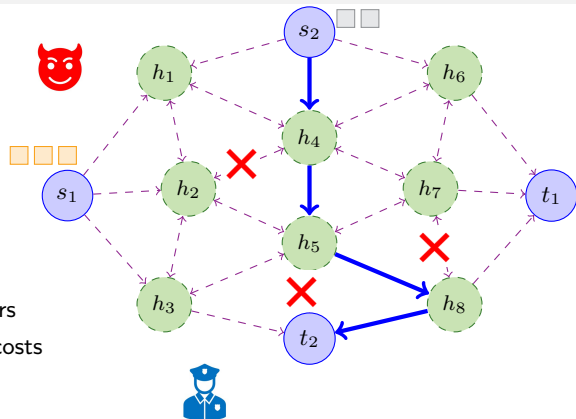
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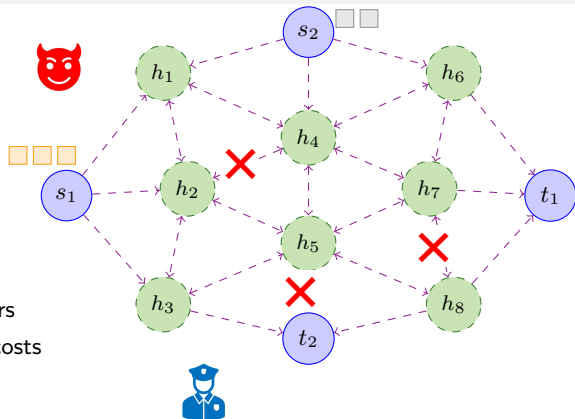
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- $x_{i,j} \in \{0, 1\}$ : Arc  $(i, j)$  is interdicted .
- $f_{i,j}^p \in \mathbb{R}_{\geq 0}$ : Commodity flow on arc  $(i, j)$  for O-D pair  $p$ .



# Network Interdiction Problem - Formulation

$\mathcal{P}$  : Set of O-D pairs

$\mathcal{H}$  : Set of hubs

$\mathcal{A}$  : Set of transportation arcs

$d_p$  : Commodity demand  
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# Network Interdiction Problem - Formulation

subject to:

$$x_{i,j} \in \{0, 1\},$$

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Dual of the inner problem

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## Single-level mixed integer program

$$\max_{x, \pi} \sum_{p \in \mathcal{P}} (\pi_s^p - \pi_t^p)$$

s.t:

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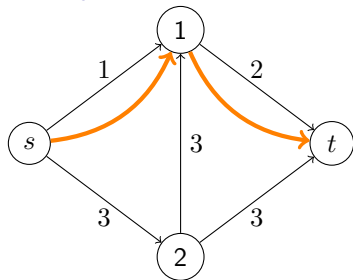
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**Large # variables:** Problem size reduction required

# Edge Interdictions

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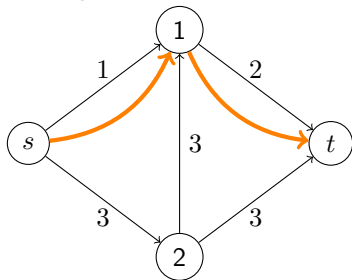


Shortest Path Length: 3

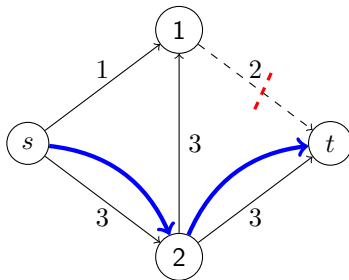
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# Edge Interdictions

- Examples:



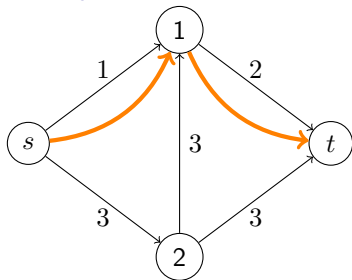
Shortest Path Length: 3  
# Edge interdictions: 0



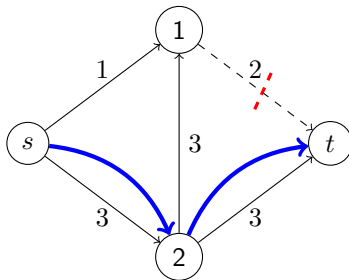
Shortest Path Length: 5  
# Edge interdictions: 1

# Edge Interdictions

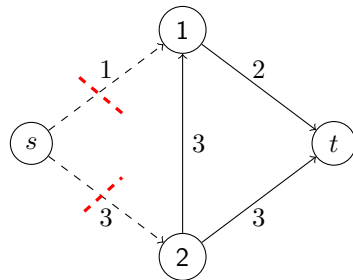
- Examples:



Shortest Path Length: 3  
# Edge interdictions: 0



Shortest Path Length: 5  
# Edge interdictions: 1

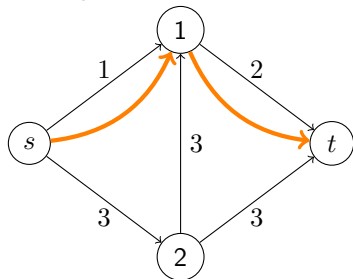


Shortest Path Length:  $\infty$   
# Edge interdictions: 2

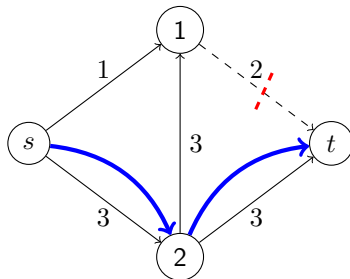


# Edge Interdictions

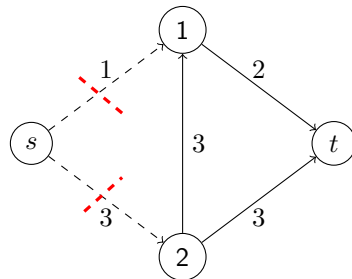
- **Examples:**



Shortest Path Length: 3  
# Edge interdictions: 0



Shortest Path Length: 5  
# Edge interdictions: 1



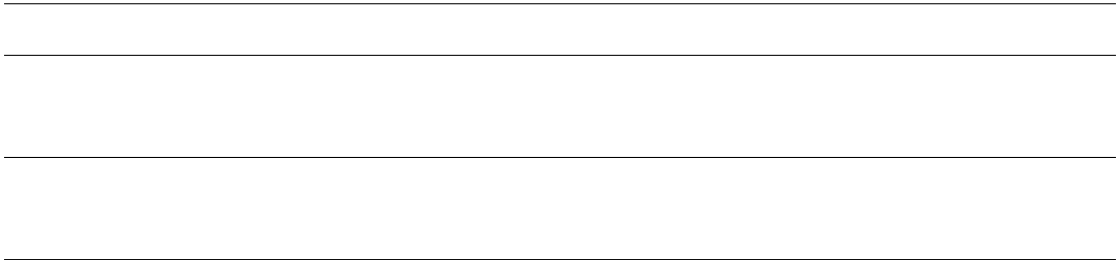
Shortest Path Length:  $\infty$   
# Edge interdictions: 2

- Which edge(s) to interdict depends upon the **resource availability** at adversary
- **Problem size reduction:** Not generating arc variables that won't be interdicted
  - Search tree to find out such arcs

# Case Study

- Major Parcel Delivery Company in China
  - Several millions of parcels handled every week
  - **Implementation Scale:** Central China
- Potential locations for logistics hub construction
  - **Logistics significance:** Major cities, highway intersections, and existing city-based inbound/outbound hubs
- Regulations set by Chinese government
  - 11-hour driving limit per day
  - **Allowable transportation edges:** 5.5 hours of travel time
- Topology-optimized networks designed through minimizing
  - single shortest path - Lean network
  - $k$ -shortest paths
  - $k$ -shortest edge-disjoint path

# Computational Performance



# Computational Performance

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**Method**

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Pre-processing +  
Gurobi

---

Gurobi

---

# Computational Performance

Method	# Hubs	$ \mathcal{A} $
	60	1005
Pre-processing + Gurobi	70	1074
	80	1344
	90	1429
	60	1005
Gurobi	70	1074
	80	1344
	90	1429

# Computational Performance

Method	# Hubs	$ \mathcal{A} $	$ \mathcal{A}' $
Pre-processing + Gurobi	60	1005	586
	70	1074	656
	80	1344	767
	90	1429	817
Gurobi	60	1005	-
	70	1074	-
	80	1344	-
	90	1429	-

# Computational Performance

Method	# Hubs	$ \mathcal{A} $	$ \mathcal{A}' $	# Variables
Pre-processing + Gurobi	60	1005	586	3137
	70	1074	656	3227
	80	1344	767	3312
	90	1429	817	3403
Gurobi	60	1005	-	18207
	70	1074	-	18641
	80	1344	-	21290
	90	1429	-	23388

# Computational Performance

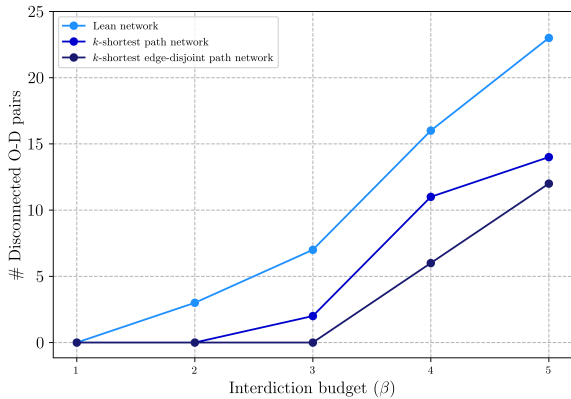
Method	# Hubs	$ \mathcal{A} $	$ \mathcal{A}' $	# Variables	# Constraints
Pre-processing + Gurobi	60	1005	586	3137	4288
	70	1074	656	3227	4571
	80	1344	767	3312	4836
	90	1429	817	3403	5912
Gurobi	60	1005	-	18207	150,976
	70	1074	-	18641	163,420
	80	1344	-	21290	212,830
	90	1429	-	23388	261,777



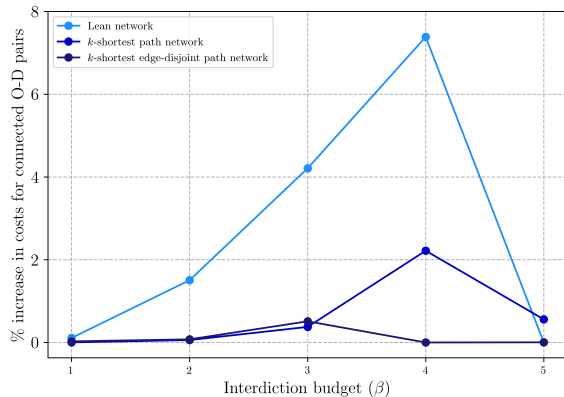
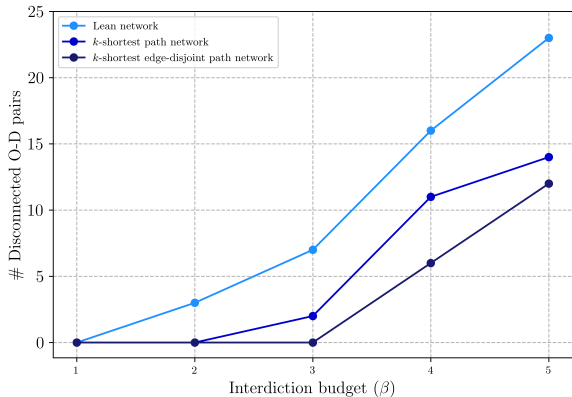
# Computational Performance

Method	# Hubs	$ \mathcal{A} $	$ \mathcal{A}' $	# Variables	# Constraints	Total Time (sec)	Optimality Gap (%)
Pre-processing + Gurobi	60	1005	586	3137	4288	54	0
	70	1074	656	3227	4571	59	0
	80	1344	767	3312	4836	62	0
	90	1429	817	3403	5912	82	0
Gurobi	60	1005	-	18207	150,976	time limit	504.5
	70	1074	-	18641	163,420	time limit	831.4
	80	1344	-	21290	212,830	time limit	1392.5
	90	1429	-	23388	261,777	time limit	1965.2

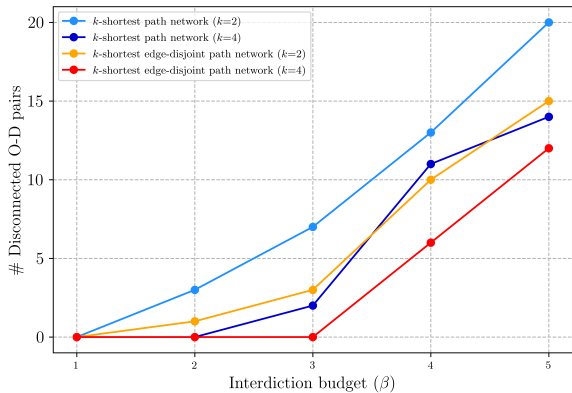
# Resilience Analysis of Networks



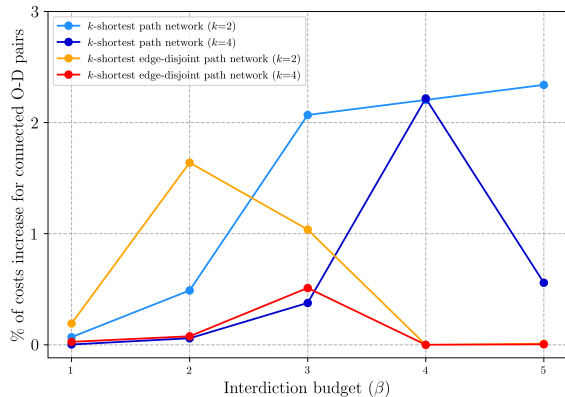
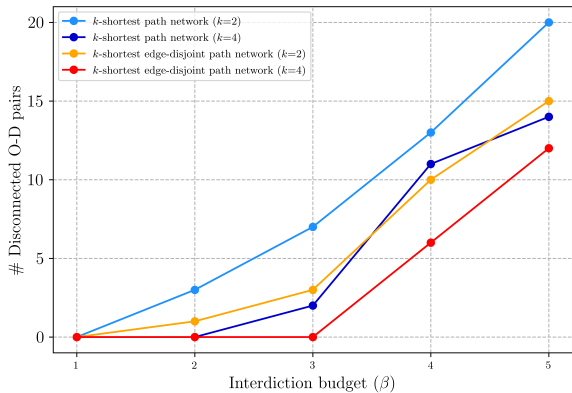
# Resilience Analysis of Networks



# Resilience Analysis of Networks



# Resilience Analysis of Networks



# Summary

## Contributions:

- Resilience assessment of large-scale networks under worst-case disruptions
- Network interdiction problem with a bi-level mixed integer formulation
- Dualization procedure and search tree strategy to reduce the problem size drastically
- Computational performance comparison of the solution methodology against off-the-shelf solver
- Resilience analysis of the topology-optimized networks

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- Hub sizes consideration in modelling
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## Future work:

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*Thank you!*

Questions: [onkar.kulkarni@gatech.edu](mailto:onkar.kulkarni@gatech.edu)