



**IPIC 2023**

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# Hyperconnected Urban Parcel Network Design with Tight Delivery Service Requirements

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Joint work with

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La Poste Group

**13-15 JUNE 2023** Athens, Greece  
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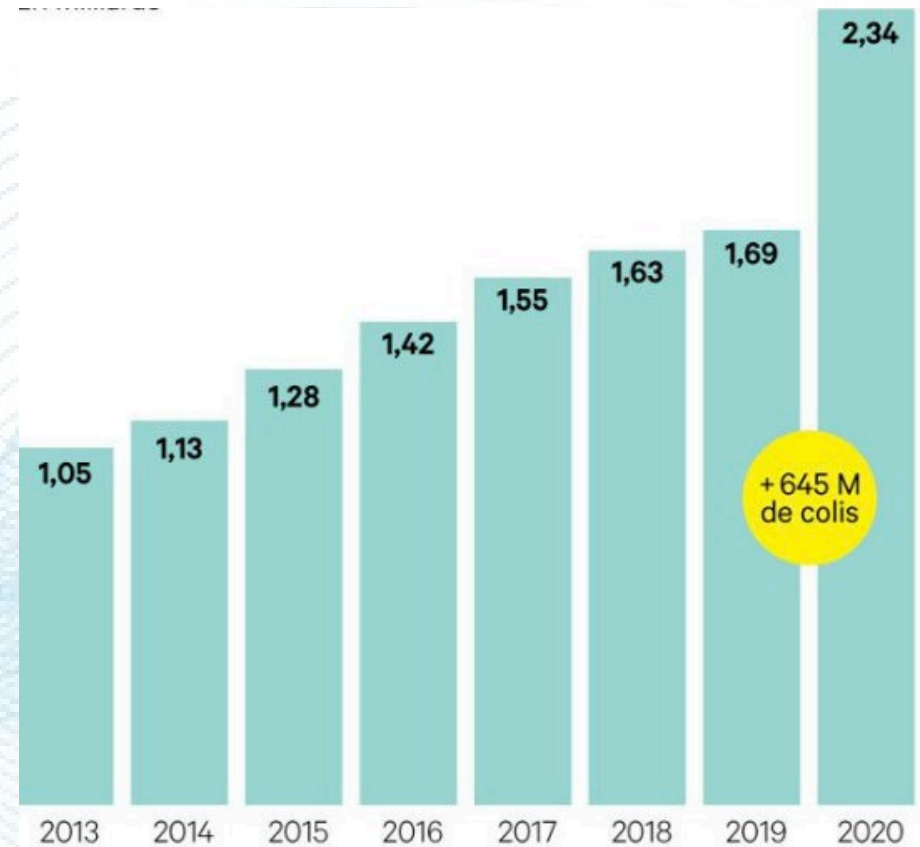
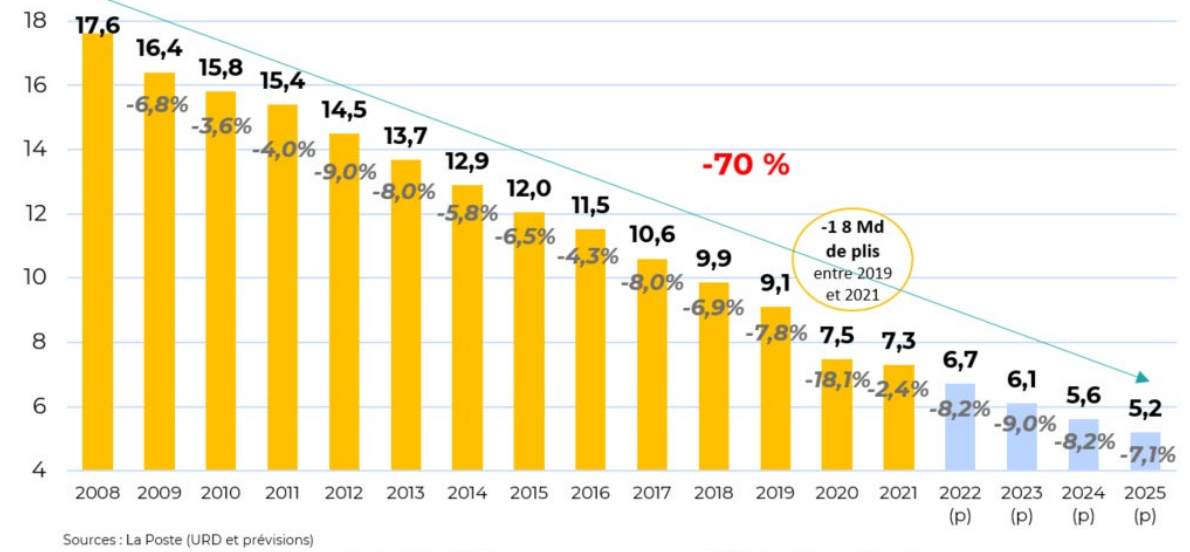
**Expanding the logistics Scope**

# Context

La Poste's network is in deep transformation.

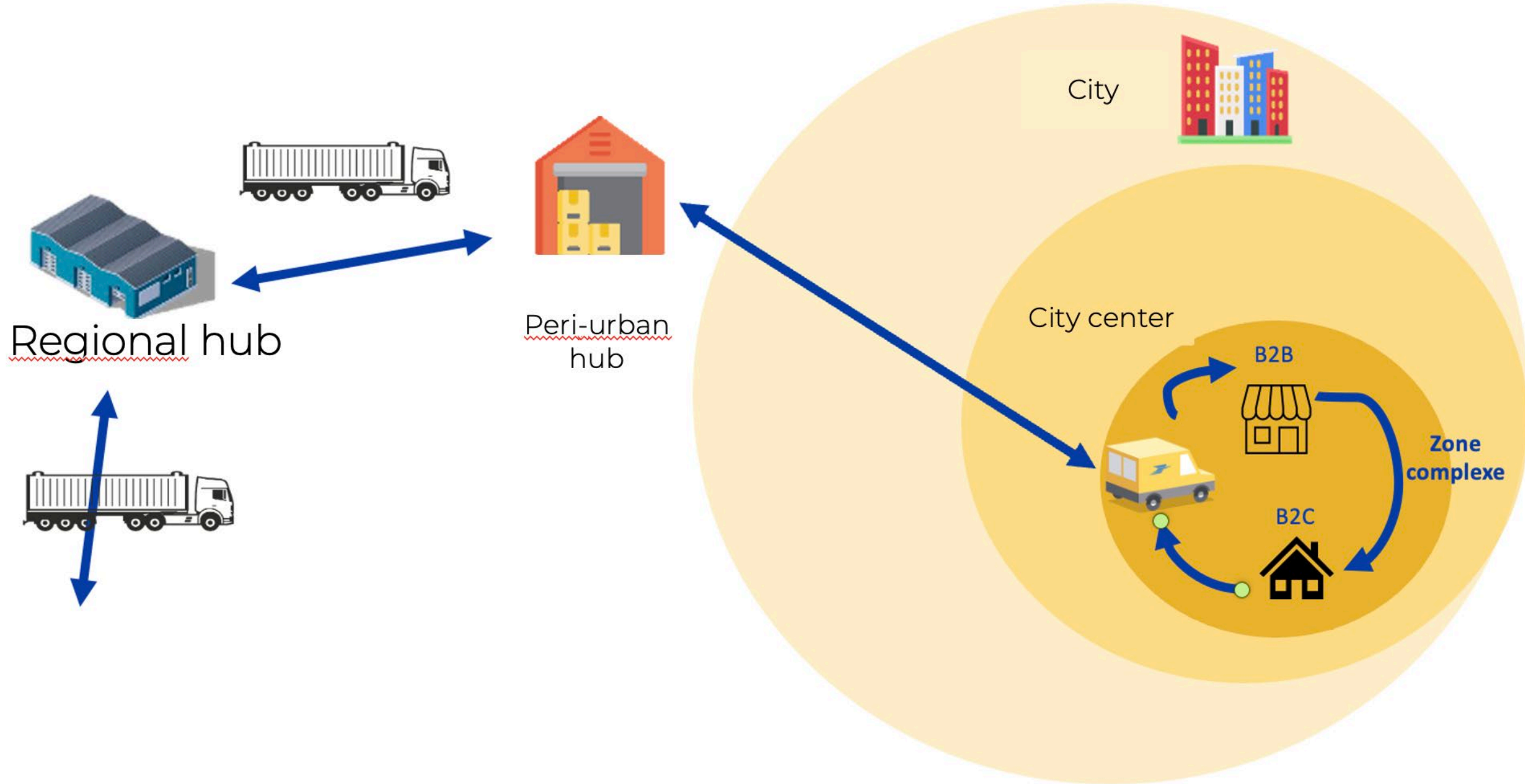


-60 % de volumes courrier adressé de 2008 à 2021

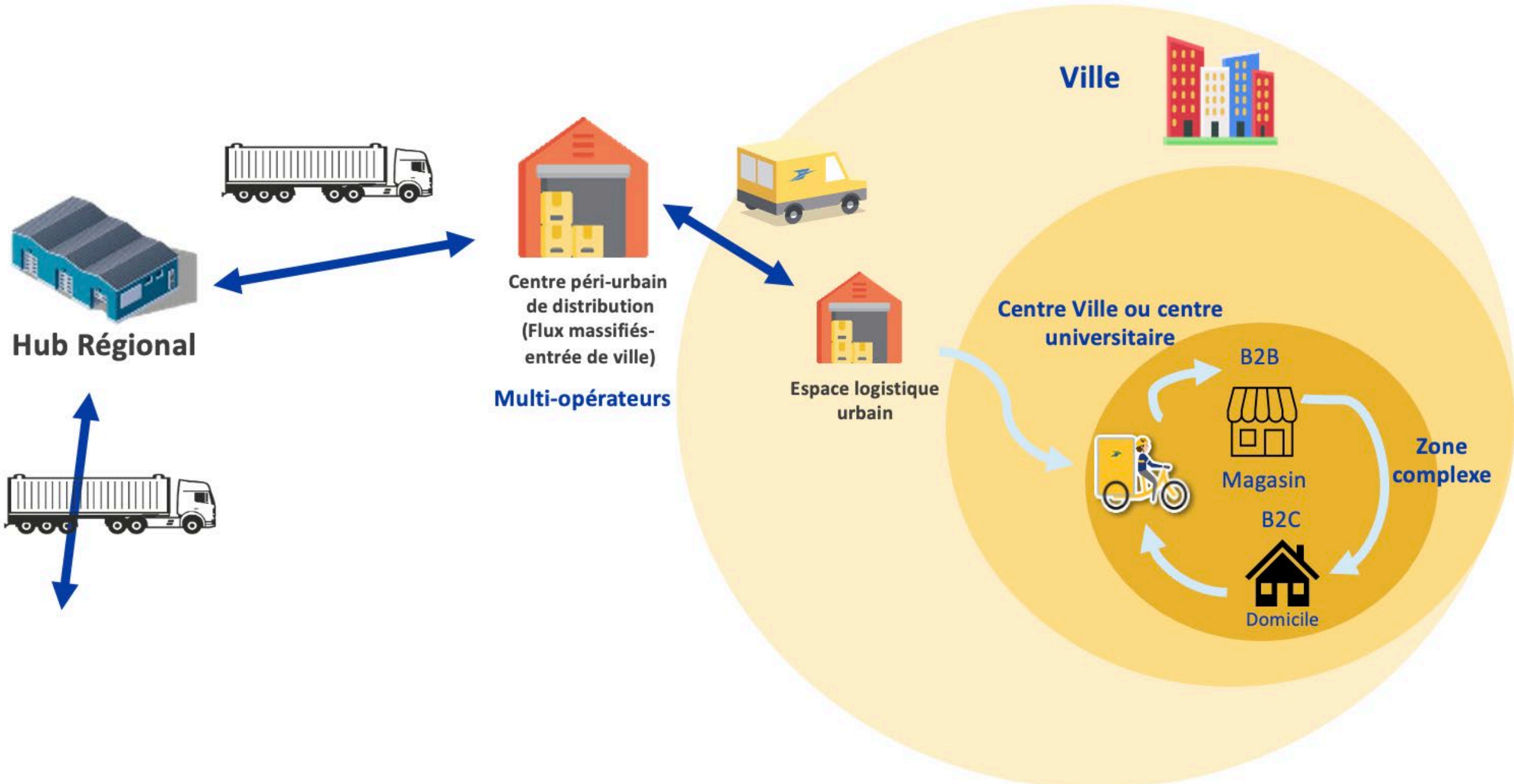




# Historical delivery network

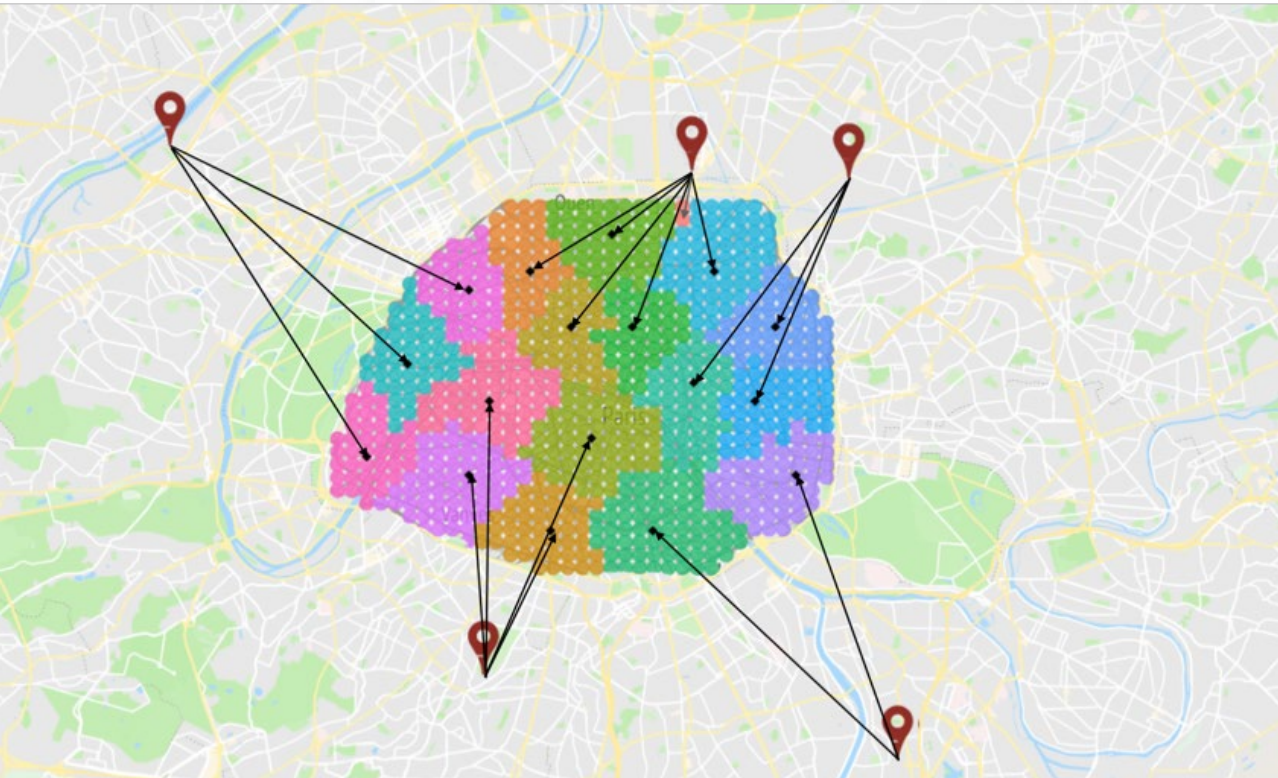


# Current delivery network





# Emerging quick markets



BFMTV

## L'hypercroissance du E-commerce : un challenge pour les ...

Le développement du « Ship from store » complexifie les plans de transport avec l'utilisation de plusieurs prestataires du dernier kilomètre. La ...

Il y a 1 jour



PR Newswire

## Same Day Delivery Market Size to hit \$ 16739 Million by 2027 ...

The same day delivery is very fast process so to avoid mix-ups if product ordered before noon are delivered on same day otherwise next morning ...

Il y a 3 semaines



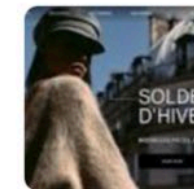
E-marketing

## Ship-from-store : ba&sh multiplie ses ventes en ligne par 3,5

...

Ship-from-store : ba&sh multiplie ses ventes en ligne par 3,5 le premier jour des soldes. Publié par Clément Fages le 1 mars 2021 | Mis à jour le 5 mars 2021 à ...

Il y a 1 mois



Voxlog

## Electro Dépôt déploie le ship-from-store avec Woop

Depuis la mi-novembre, l'enseigne de multimédia et d'électroménager a pu déployer une solution de livraison ship-from-store depuis ses 81 ...

20 janv. 2021



X



# Emerging quick markets



BFMTV

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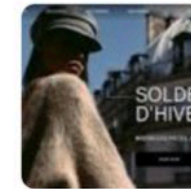
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20 janv. 2021



X

# La Poste's Group organization

## Historical role



Parcel delivery historical French main actor



International parcel express delivery



International oversize parcel delivery

They all have an already established network, why not sharing it ?



# La Poste's Group organization

La Poste has several twin companies, with their own already established networks



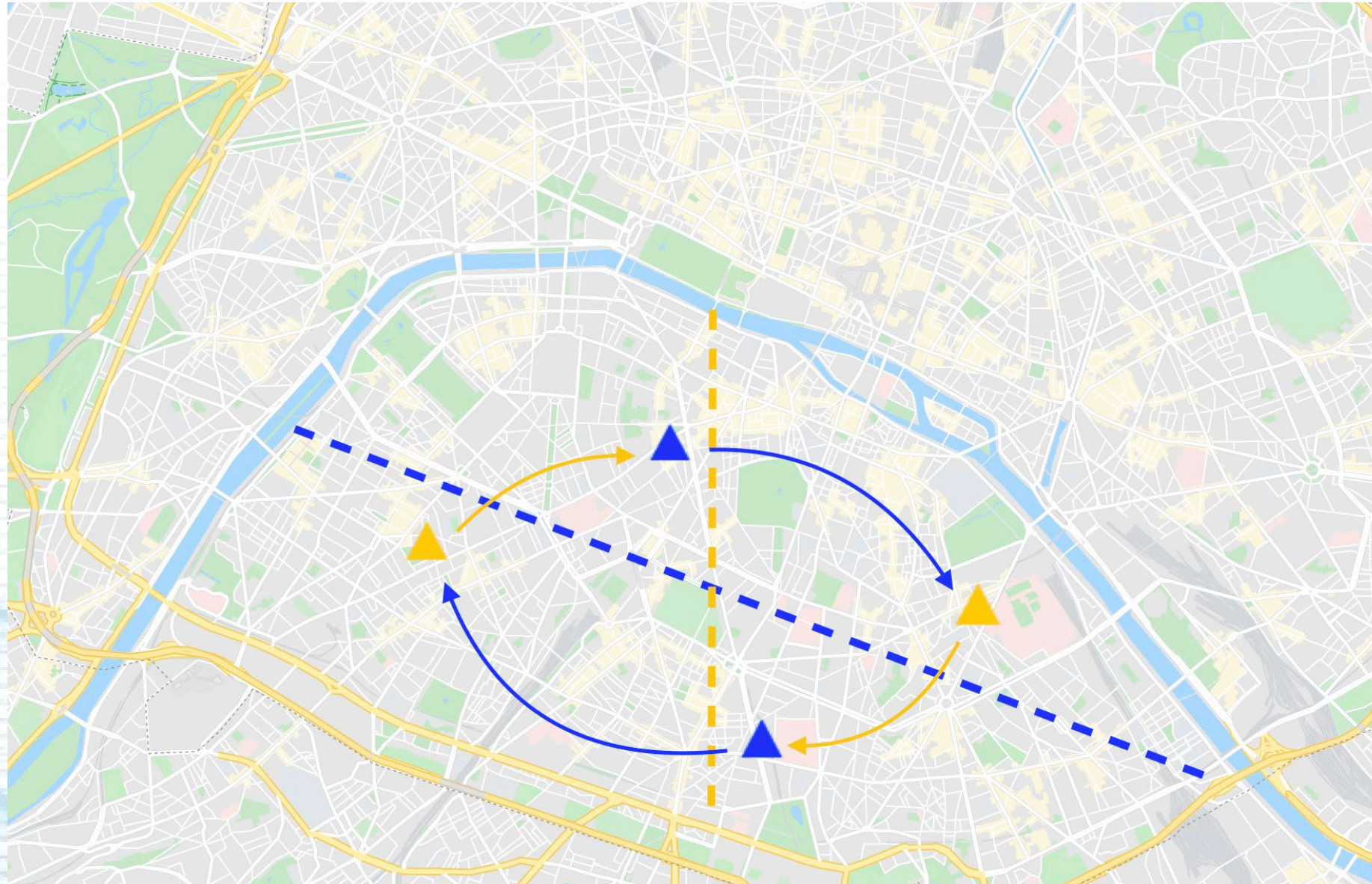
 **chronopost**



 **colissimo**

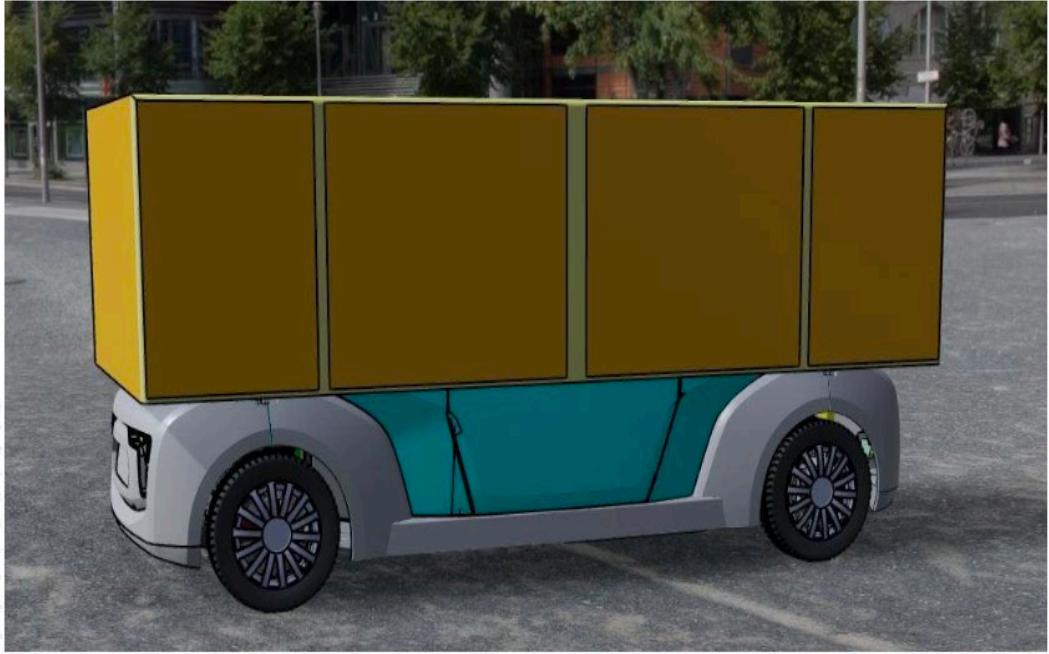


# Natural overlapping



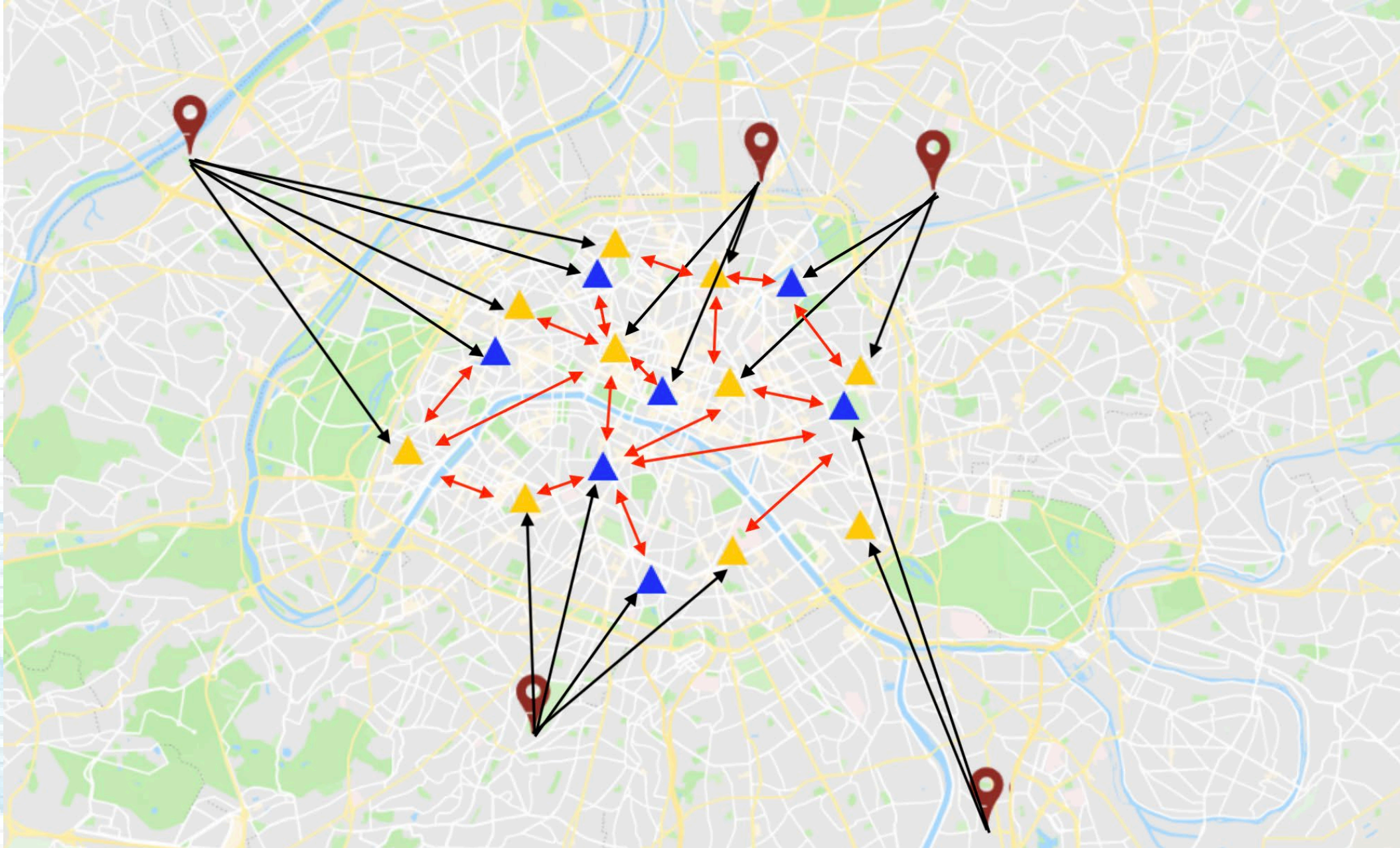


# The introduction of new delivery methods allows a higher agility



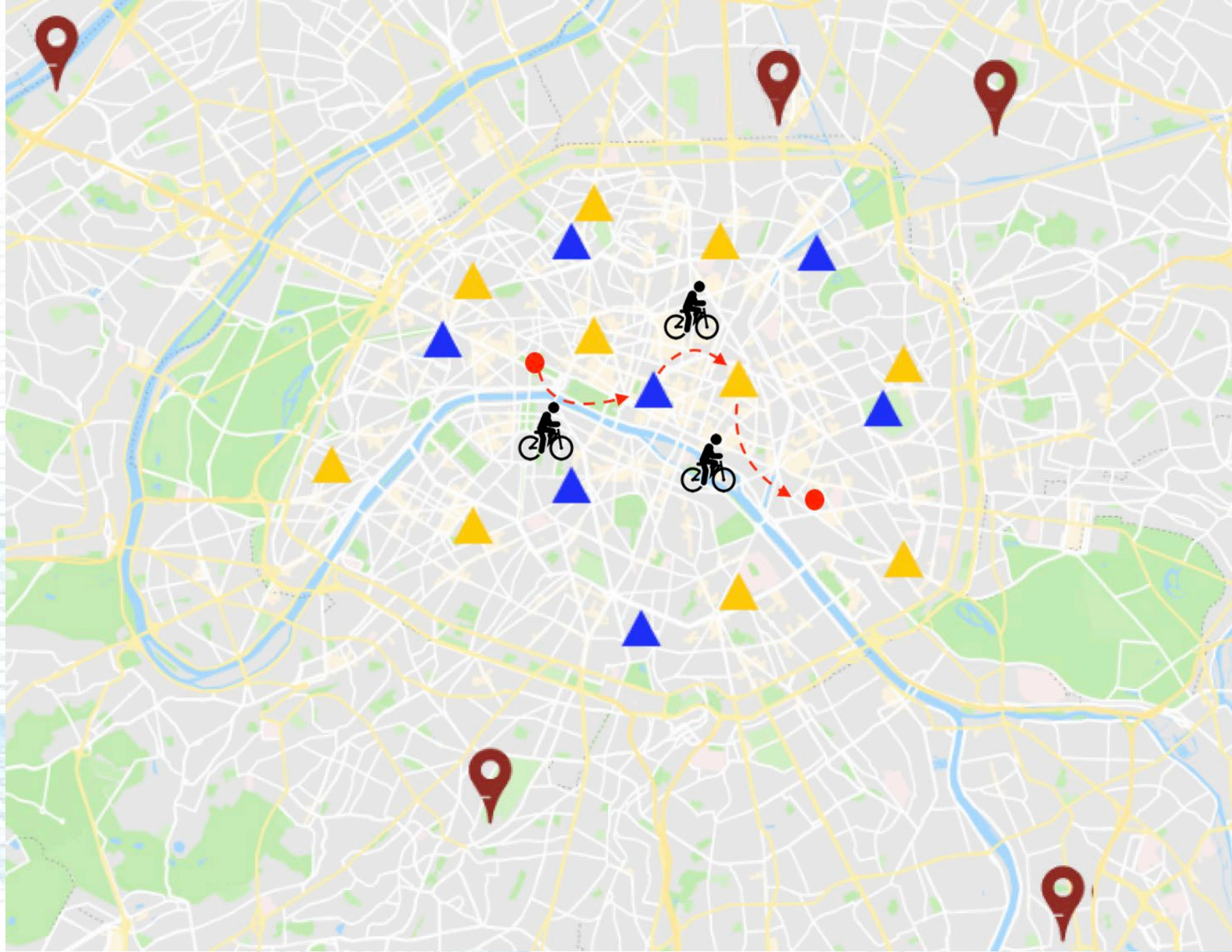


# Introduction of interconnected networks



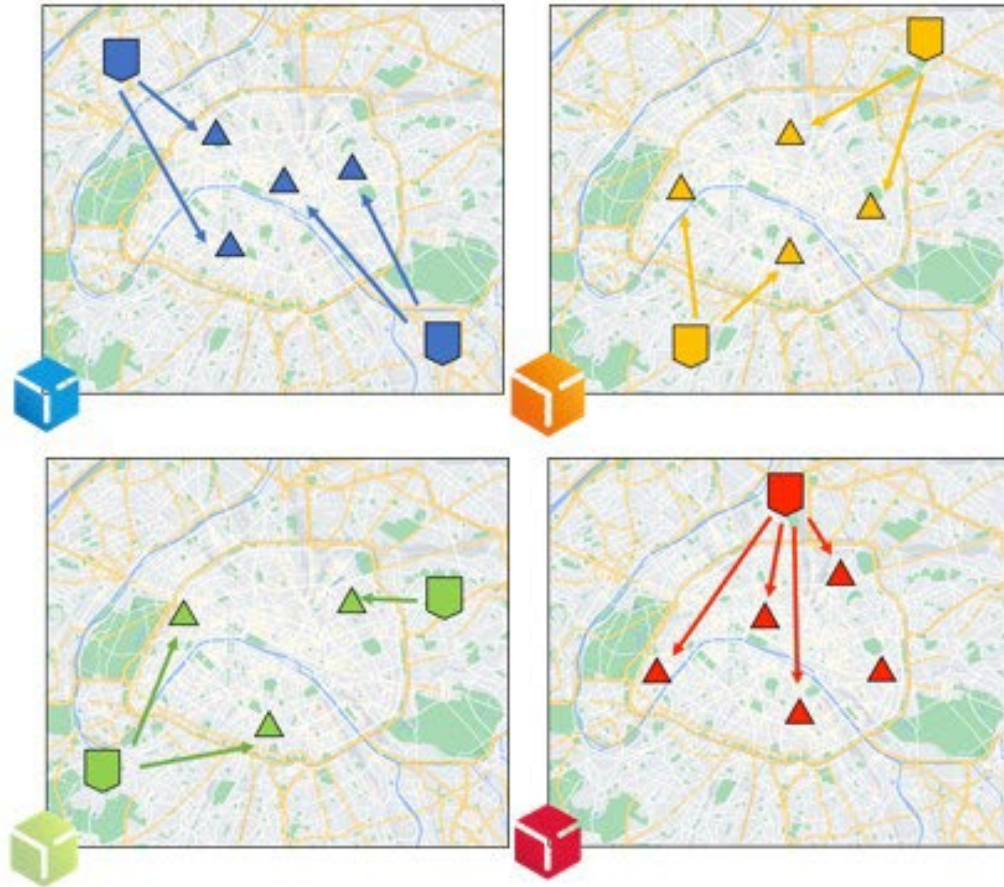


# Introduction of interconnected networks



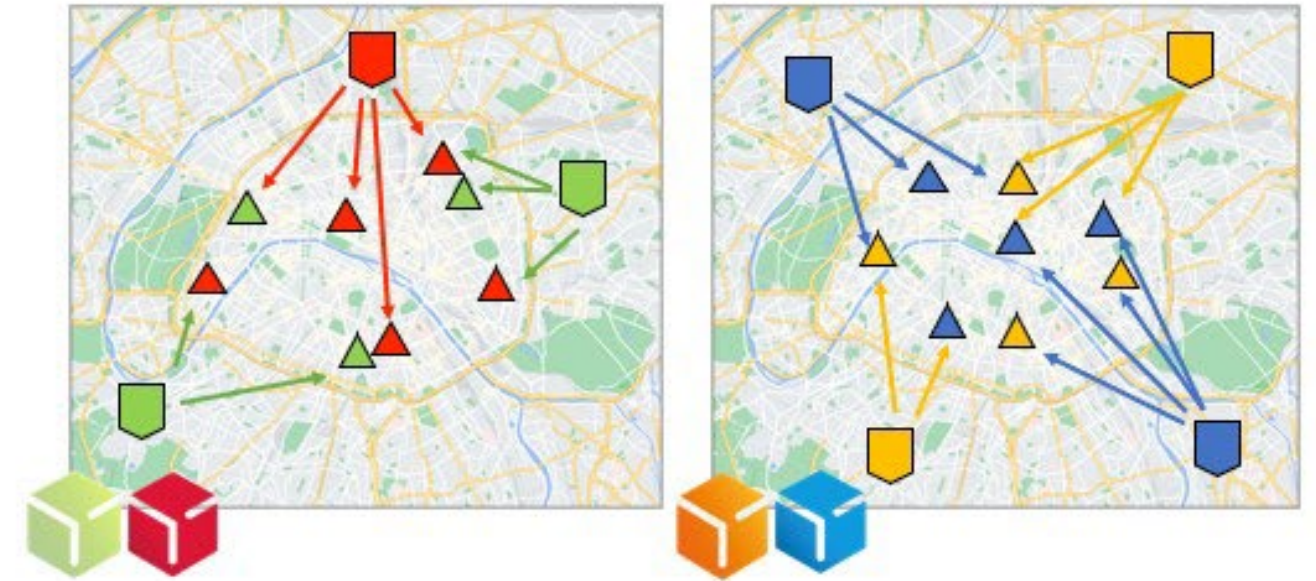


# Idea of coalition formation



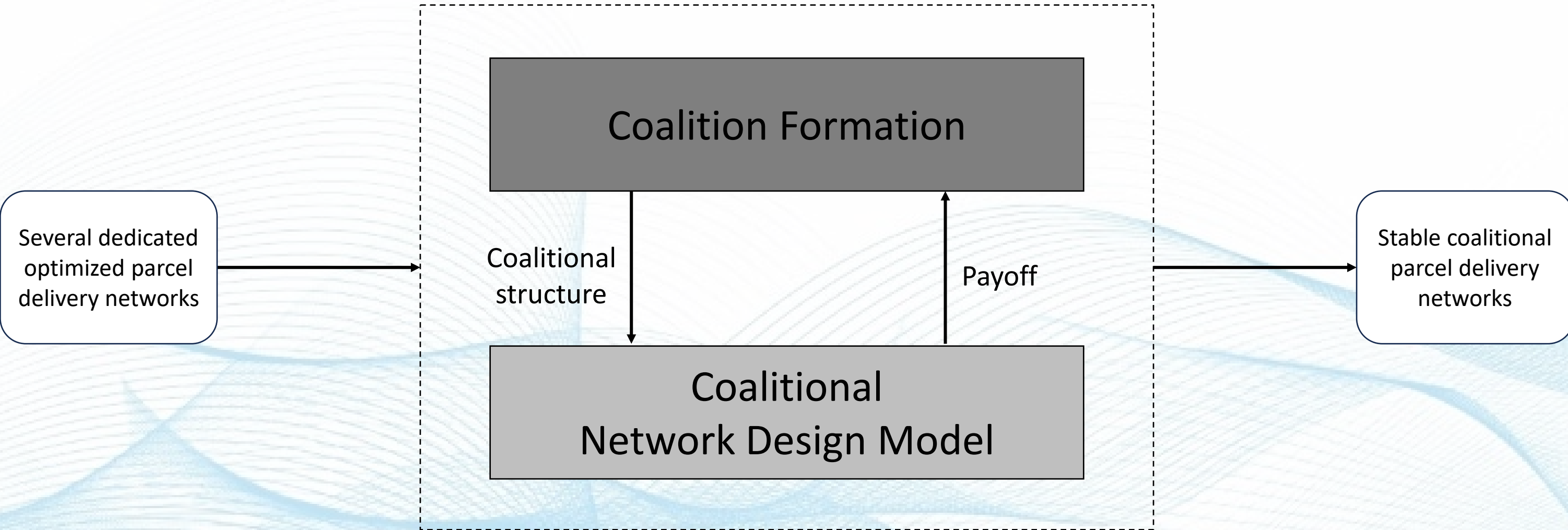
Set of delivery actors with their own dedicated parcel delivery networks

Coalition-Formation



Set of coalitions of actors with shared parcel delivery networks

# Coalitional Decision-Making Framework



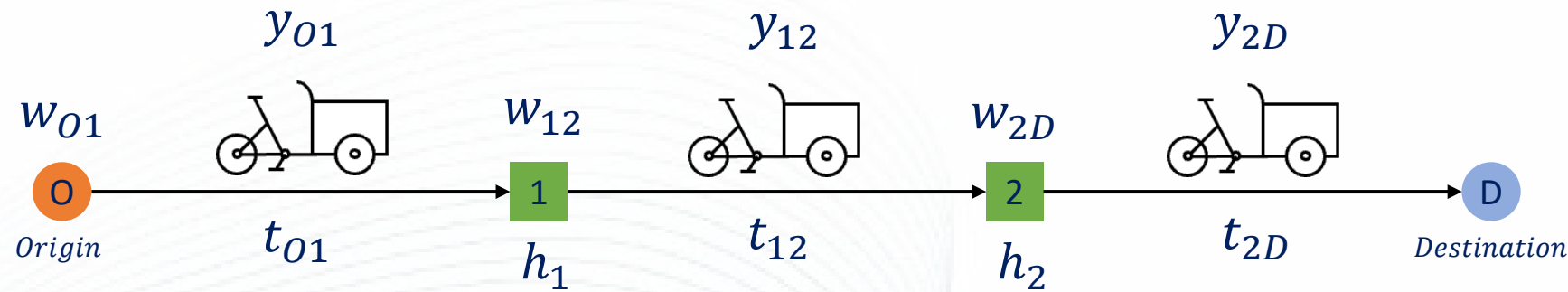
- (1) Which profitable coalitions?
- (2) How to design the coalitional network of each coalition
- (3) How to allocate the joint costs of the coalitional network between actors



# Coalitional Network Design

- **Aim:**
  - Design a coalitional urban parcel delivery network for a given coalition to enable tight delivery service requirements in a cost minimization manner
  
- **Model and Decisions:**
  - Path-based IP and frequency-based model on a flat network
  - Decisions
    - Which hubs to activate → micro-hub network decisions
    - How many vehicle dispatches along each arc per unit time → vehicle frequency decisions

# Modelling Delivery Service Requirements



- $\tau_k$ : Service requirements of O-D commodity  $k$
- $t_a$ : Travel time on arc  $a$
- $h_i$ : Hub processing time at micro hub  $i$
- $y_a$ : # of cargo bikes over arc  $a$  per time unit
- $w_a$ : Dwell time before traversing arc  $a$

**Assumptions** (Dayarian et al., (2022) , Greening et al., (2022))

- Each O-D commodity arrives at its origin according to a uniform distribution
- Cargo bikes are dispatched between locations according to a uniform distribution

⇒ Dwell time before traversing arc  $a$  is  $w_a \sim \text{Uniform}(0, \frac{1}{y_a})$  with avg. of  $\frac{1}{2} \cdot \frac{1}{y_a}$

$$\sum_{a \in p} t_a + \sum_{i \in p} h_i + \sum_{a \in p} \mathbb{E}[w_a] \leq \tau_k \Rightarrow \sum_{a \in p} \frac{1}{2} \cdot \frac{1}{y_a} \leq \hat{\omega}_{kp} = \tau_k - \left( \sum_{a \in p} t_a + \sum_{i \in p} h_i \right)$$

Total allowable dwell time  
along path  $p$  for commodity  $k$



# Coalitional Network Design Model with TDSR

## ➤ Data:

- $\mathcal{S}$ : Set of coalitions
- $\mathcal{N}^s$ : Set of hubs for coalition  $s \in \mathcal{S}$
- $\mathcal{A}^s$ : Set of arcs for coalition  $s \in \mathcal{S}$
- $\mathcal{K}^s$ : Set of commodities (O-D pairs) for coalition  $s \in \mathcal{S}$
- $\mathcal{P}_k^s$ : Set of pregenerated paths for commodity  $k \in \mathcal{K}$  for coalition  $s \in \mathcal{S}$

## ➤ Decisions for coalition $s \in \mathcal{S}$ :

- $x_h^s \in \{0,1\}$ : Hub selection
- $y_a^s \in \mathbb{Z}_{\geq 0}$ : # of CBs over arc  $a$
- $z_{kp}^s \in \{0,1\}$ : Path selection of commodity  $k$

$$\min \quad \sum_{h \in \mathcal{N}^s} f_h \cdot x_h^s + \sum_{a \in \mathcal{A}^s} g_a \cdot y_a^s$$

$$\text{s.t.} \quad \sum_{p \in \mathcal{P}_k^s} z_{kp}^s = 1, \quad \forall k \in \mathcal{K}^s$$

$$\sum_{k \in \mathcal{K}^s} \sum_{p \in \{p \in \mathcal{P}_k^s : a \in p\}} q_k \cdot z_{kp}^s \leq v \cdot y_a^s, \quad \forall a \in \mathcal{A}^s$$

$$\sum_{a \in p} \frac{1}{2} \cdot \frac{1}{y_a^s} \leq \hat{\omega}_{kp} + M \cdot (1 - z_{kp}^s), \quad \forall k \in \mathcal{K}^s, p \in \mathcal{P}_k^s$$

$$Q_i^{\min} \cdot x_i^s \leq \sum_{a \in \delta^+(i)} y_a^s \leq Q_i^{\max} \cdot x_i^s, \quad \forall i \in \mathcal{N}^s$$

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# Case Study

Table 1: Summary of parcel delivery actors

- French urban megacity (Paris)
  - 412 demand zones
  - Order of 1.6 million parcels weekly across 52k origin-destination (O-D) pairs
- French parcel/postal company
  - 3 subsidiaries of parcel delivery actors
  - Each actor offers tight delivery service requirements
    - 6,12,24,48-hour delivery
- 3 Cost-sharing methods to compute marginal cost
  - Shapley cost allocation
    - Weighted average of all marginal cost to all possible coalitions
  - Proportional fairness allocation
    - Allocation proportional to total commodity volume
  - Egalitarian allocation
    - Equal Allocation

| Delivery actor | # of Micro-hubs | Market Share | # of OD Commodities |
|----------------|-----------------|--------------|---------------------|
| 1              | 19              | 60%          | 35591               |
| 2              | 3               | 10%          | 6162                |
| 3              | 8               | 30%          | 18105               |



# Case Study: Cost-Sharing Methods

## Input:

$S$ : Set of coalitions

$I$ : Set of actors

$I^s$ : Set of actors in coalition  $s \in S$

$M$ : Set of cost-sharing methods

= {Shapley, PF, Eg}

$K_i$ : Set of commodities for actor  $i$

$q_{ik}$ : Volume of commodity  $k$  of actor  $i$

$C_{i,s}^m$ : Marginal cost of actor  $i$  in coalition  $s$

for allocation method  $m \in M$

## Cost-Sharing Methods:

• Shapley Cost Allocation:  $C_{i,s}^{Shapley} = \sum_{\bar{I} \subseteq I^s: i \in \bar{I}} \frac{(|I^s| - |\bar{I}|)! \cdot (|\bar{I}| - 1)!}{|I^s|!} \cdot (C_{\bar{I}} - C_{\bar{I} \setminus i})$

• Proportional Fairness Allocation:  $C_{i,s}^{PF} = \frac{C_s \cdot \sum_{k \in K_i} q_{ik}}{\sum_{i' \in I^s} \sum_{k \in K_{i'}} q_{i'k}}$

• Egalitarian Allocation:  $C_{i,s}^{Eg} = \frac{C_s}{|I^s|}$

# Case Study: Global Network Design Performance

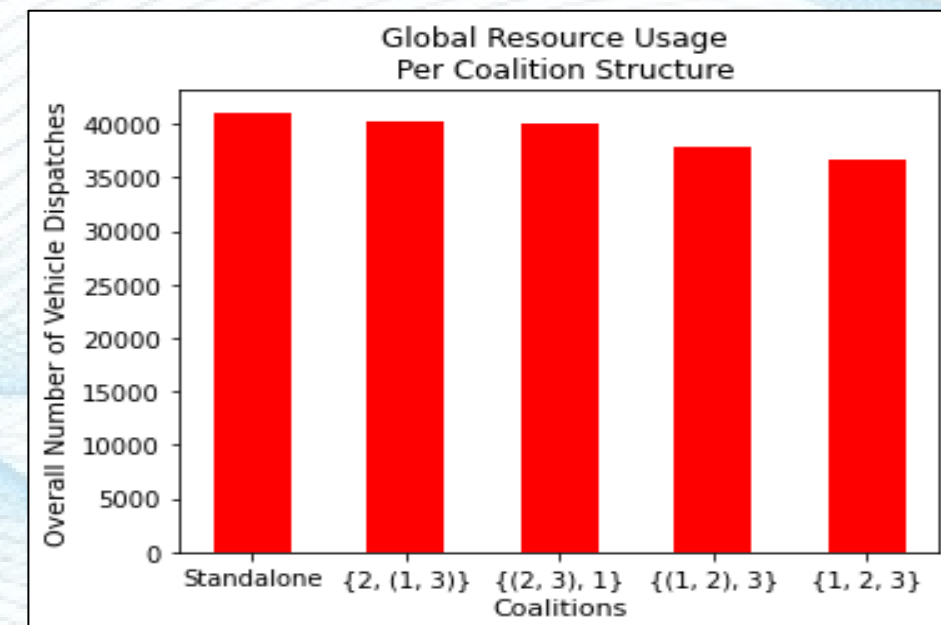
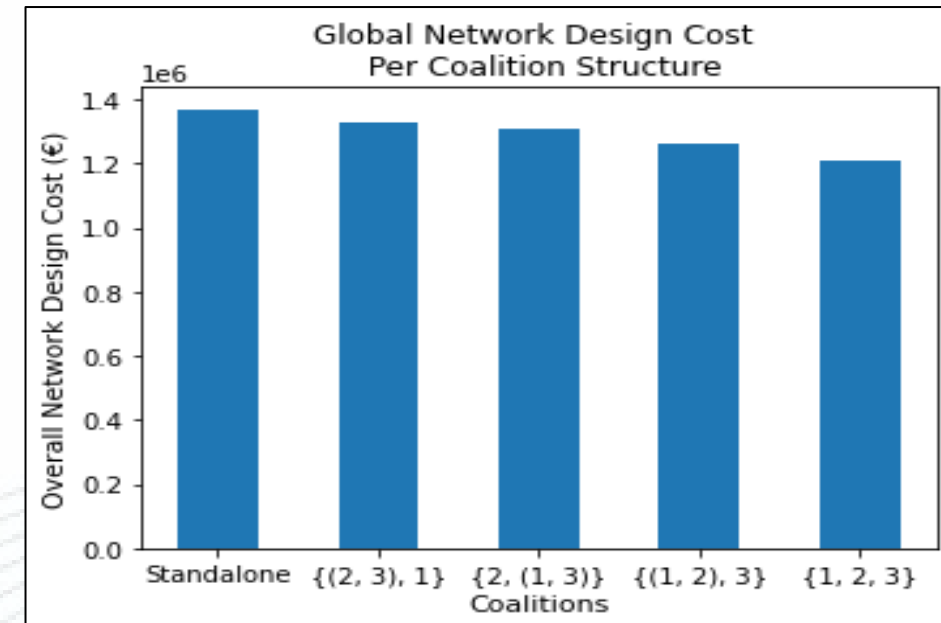
Table 1: Summary of Network Design of individual actors

| Actor | #. of open MHs | No. O-D Commodities | Cost (€)  |
|-------|----------------|---------------------|-----------|
| 1     | 19             | 35591               | 830692.29 |
| 2     | 3              | 6162                | 124791.77 |
| 3     | 8              | 18105               | 414332.01 |

Table 2: Summary of possible coalitions

| Coalition | # of potential MHs | # of open MHs | # of O-D Commodities | Description                 |
|-----------|--------------------|---------------|----------------------|-----------------------------|
| (1,2)     | 19                 | 19            | 41301                | Coalition of Actors 1 and 2 |
| (1,3)     | 27                 | 26            | 52472                | Coalition of Actors 1 and 3 |
| (2,3)     | 11                 | 11            | 24044                | Coalition of Actors 2 and 3 |
| (1,2,3)   | 30                 | 28            | 57968                | Grand Coalition             |

Figure 3: Global Network Design Performance





# Case Study: Impact of Cost-Sharing Methods

Figure 4: Allocated cost to actors per cost-sharing method

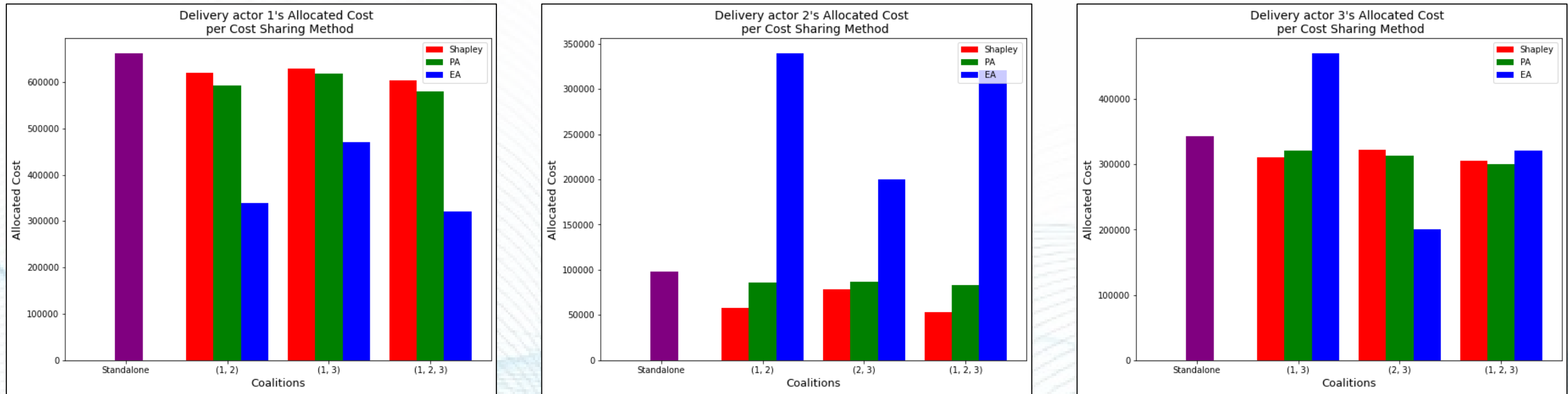
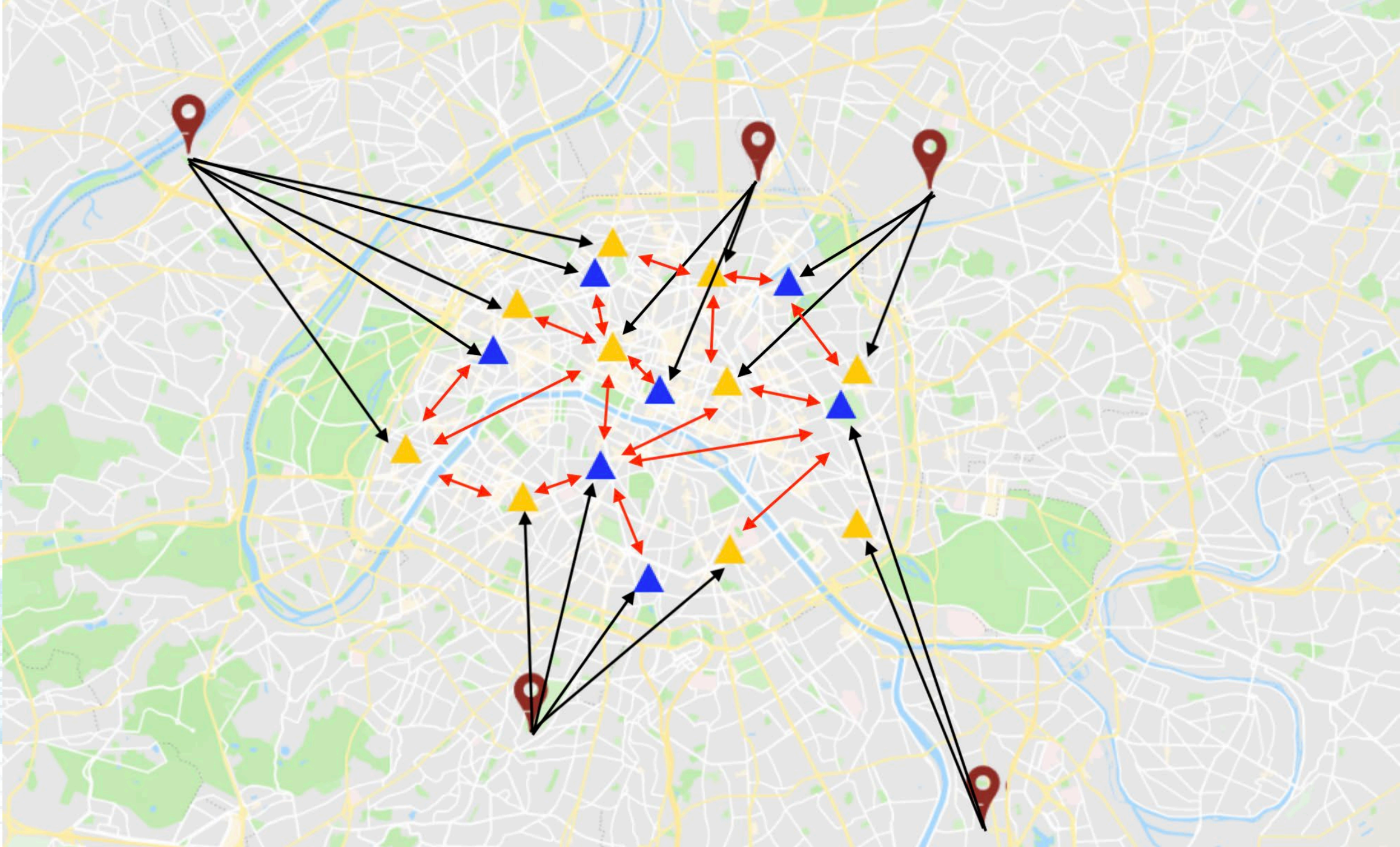


Table 3: Summary of coalitional decisions per cost-sharing method

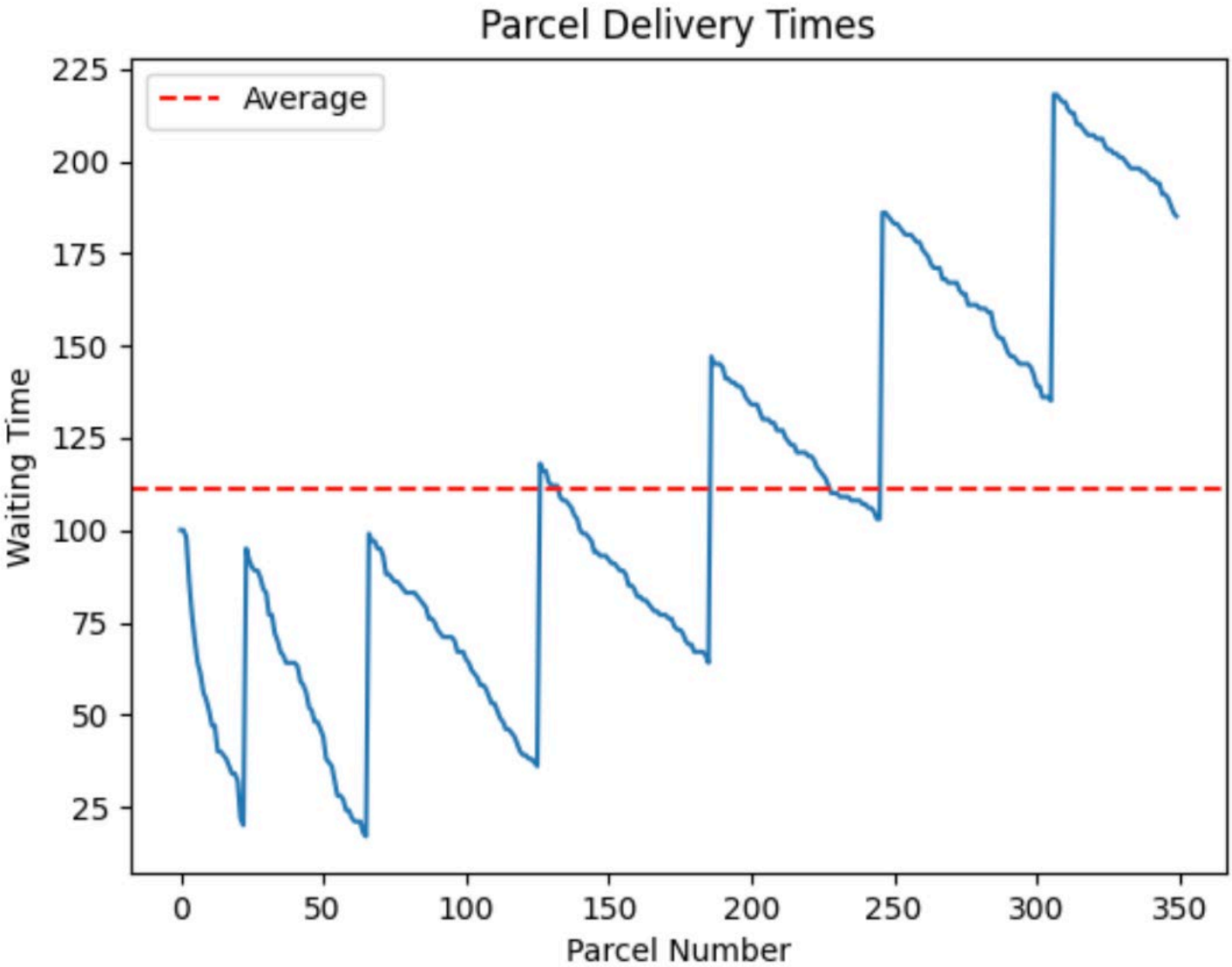
| Total No. Coalitions | Shapley         |                      |      | Proportional (PA) |                      |      | Egalitarian (EA) |                      |      |
|----------------------|-----------------|----------------------|------|-------------------|----------------------|------|------------------|----------------------|------|
|                      | No. Cop. Actors | No. Prof. Coalitions | Coal | No. Cop. Actors   | No. Prof. Coalitions | Coal | No. Cop. Actors  | No. Prof. Coalitions | Coal |
| 7                    | 3               | 5                    | 1    | 3                 | 5                    | 1    | 0                | 0                    | 3    |

# Type of connected networks





# Simulation for Robust O-D Service Guarantees



: Starts every X minutes, either full or not.

**Future work** : introduction of robust policy for vehicle dispatch

Congestion created by a fixed number of vehicles and a rigid dispatch policy

# Summary

**Thank you!**

Questions: [johan.leveque@laposte.fr](mailto:johan.leveque@laposte.fr)

**IPIC 2023**



# Robust O-D Service Guarantees

**Assumptions** (Dayarian et al., (2022) , Greening et al., (2022))

- Each O-D commodity arrives at its origin according to a uniform distribution
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⇒ Dwell time before traversing arc  $a$  is  $w_a \sim \text{Uniform}(0, \frac{1}{y_a})$  with avg. of  $\frac{1}{2} \cdot \frac{1}{y_a}$

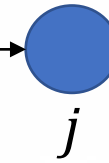
$$\sum_{a \in \rho} t_a + \sum_{i \in \rho} h_i + \sum_{a \in \rho} \mathbb{E}[w_a] \leq \tau_k \Rightarrow \sum_{a \in \rho} \frac{1}{2} \cdot \frac{1}{y_a} \leq \hat{\omega}_{kp} = \tau_k - \left( \sum_{a \in \rho} t_a + \sum_{i \in \rho} h_i \right)$$

- Vehicle dispatches ⇒ Uniform distribution
  - Restrictive
  - Over-optimistic (50%) ⇒ not robust
- Q. Is there any other way to ensure robustness in O-D service guarantees with frequency variables?

# Robust O-D Service Guarantees

$n$  demand flows

- each with volume  $q_d \forall d \in \{1, 2, \dots, n\}$
- Arriving on an interval  $[0, T]$



$k$  vehicles with capacity  $v$   
such that  $k * v \geq \sum_d q_d$



## Policy:

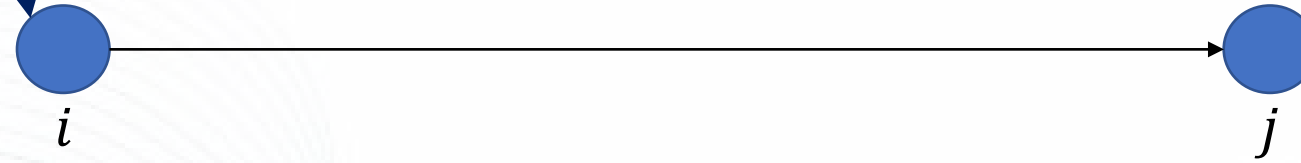
- 1<sup>st</sup> vehicle must depart **either at the latest at  $\frac{1}{k}$  time or when full**
  - $\tau_i$ : departure time of vehicle  $i$
- $i^{\text{th}}$  vehicle ( $\forall i > 1$ ) must depart **either at the latest at  $\tau_{i-1} + \frac{1}{k}$  or when full**



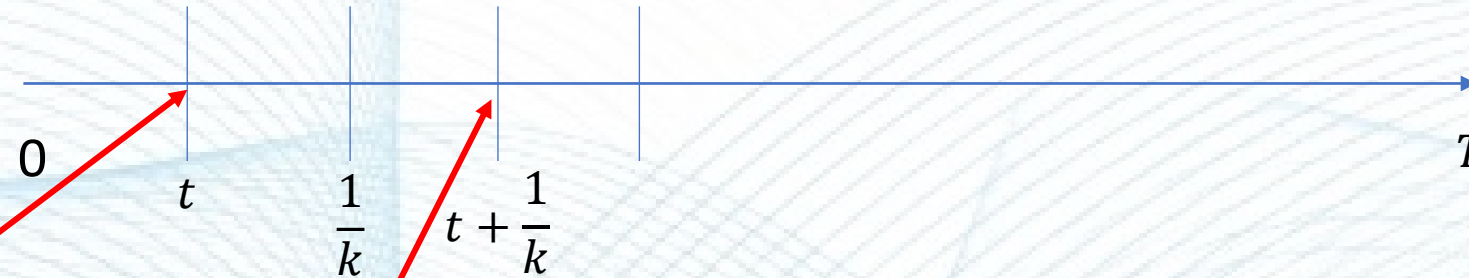
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$k$  vehicles with capacity  $v$   
such that  $k * v \geq \sum_d q_d$



If 1<sup>st</sup> vehicle leaves at  $t$   
(leaving b/c it's full)

2<sup>nd</sup> vehicle must leave by  
 $t + \frac{1}{k}$

→ No flows wait more than  $\frac{1}{k}$

→ We need at most  $2k$  vehicles to ensure waiting time  $\leq \frac{1}{k}$

- At most  $k$  vehicles for those leaving every  $\frac{1}{k}$  time, not full
- At most  $k$  vehicles for those leaving when full

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# Robust O-D Service Guarantees

what if  $k < 2$ ?

➤ Theoretically, having twice more vehicles leads to 100% O-D service guarantees

- Too conservative?
- What would happen if we only increased # of vehicles by  $k$  times?
  - $k < 2$

➤ Experiments for robustness in O-D service guarantees through simulation

- Impact of different  $k$  ( $= 2, 1.9, 1.7, 1.5, ..$ ) on robust O-D service guarantees

$$\min \sum_{h \in \mathcal{N}^s} f_h \cdot x_h^s + \sum_{a \in \mathcal{A}^s} 2 \cdot g_a \cdot y_a^s$$

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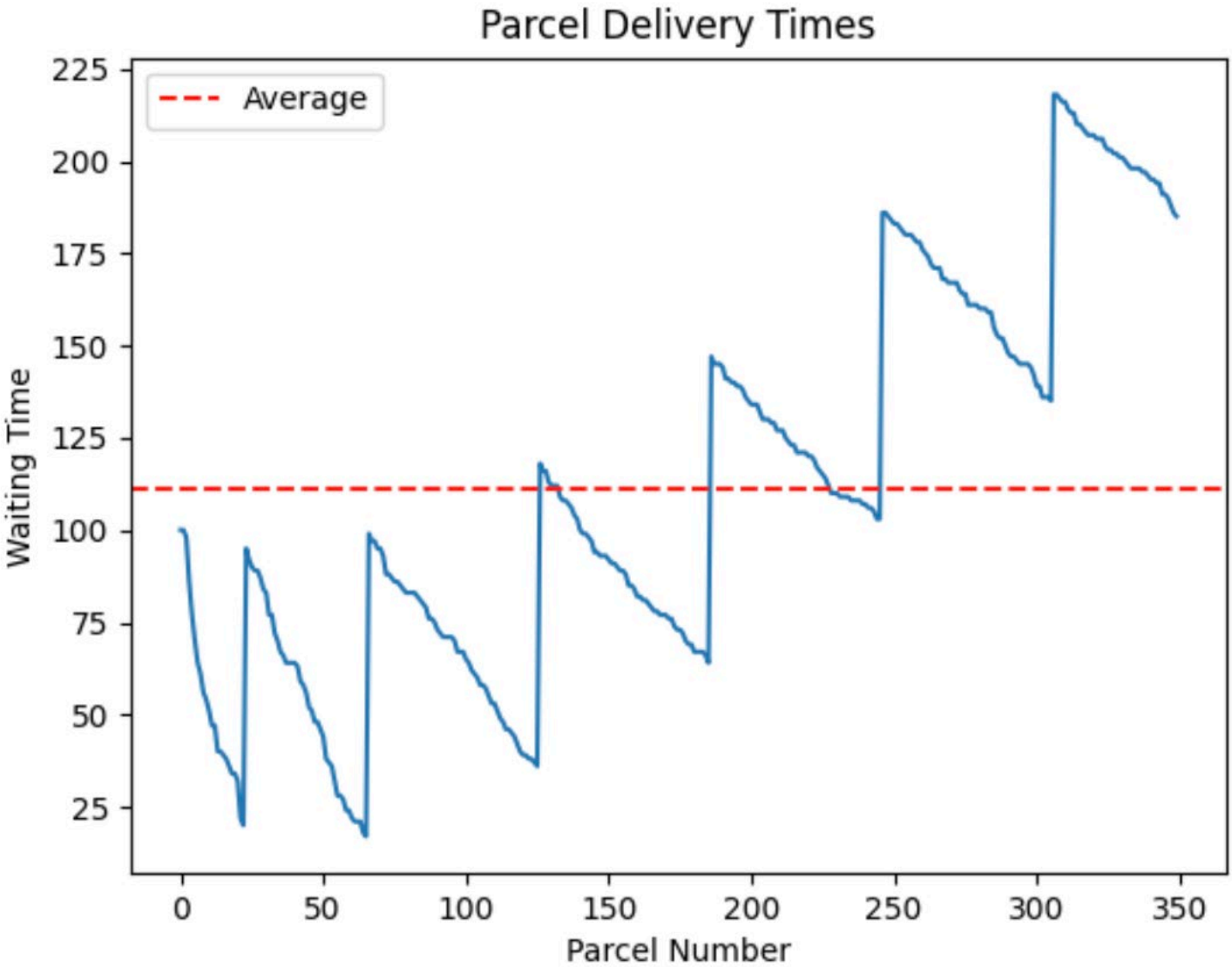
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# Simulation for Robust O-D Service Guarantees

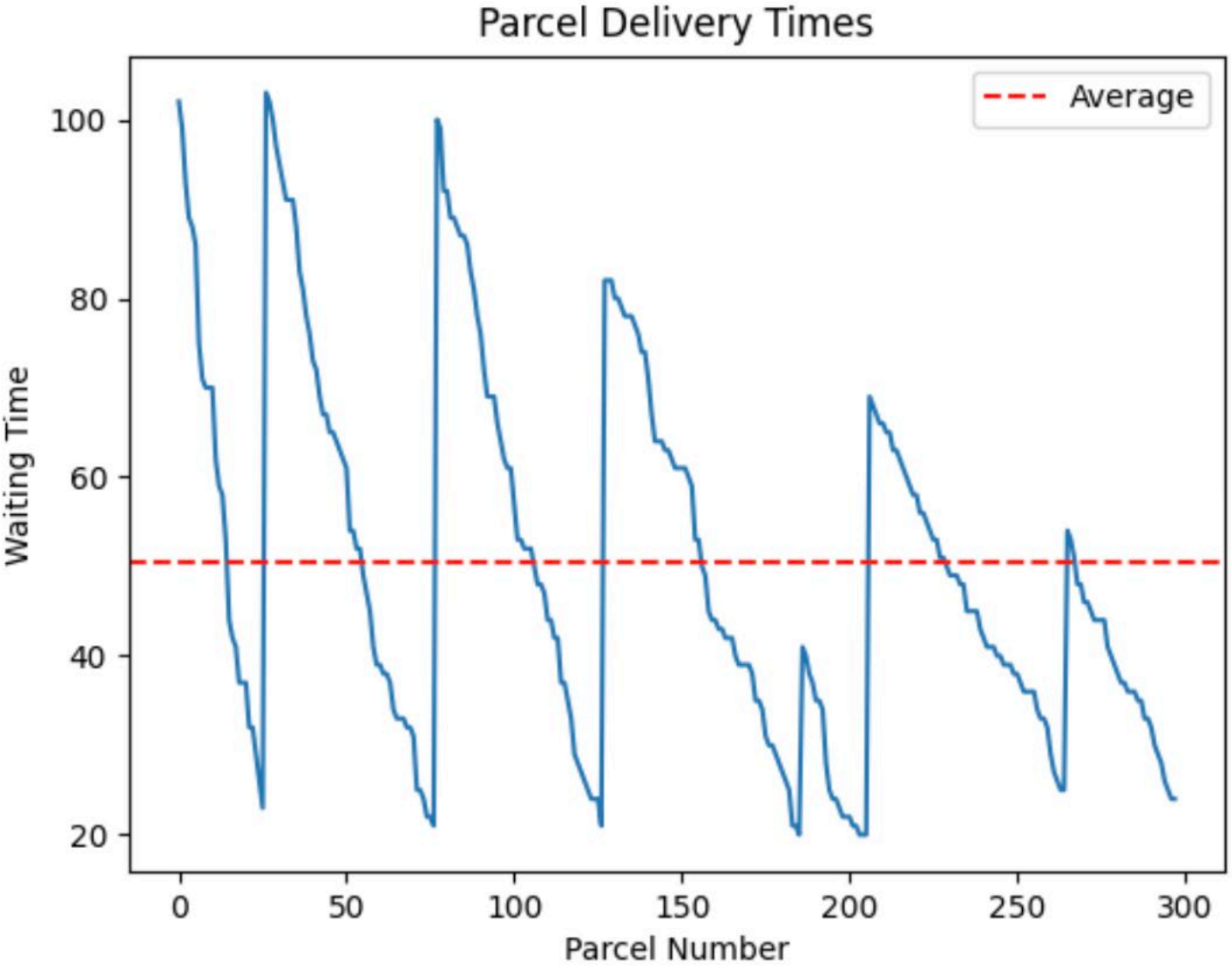


: Starts every X minutes, either full or not.

Congestion created by a fixed number of vehicles and a rigid dispatch policy



# Simulation for Robust O-D Service Guarantees



: Starts either when full or when it's time → Suppose to have twice the number of trucks. Is this really twice in practice ?

Adapted policy, delivery times are highly reduced due to an increased and flexible frequency